

## FACULTY OF ENGINEERING

B.E. (ECE) III - Semester (AICTE) (Backlog) (Old) Examination, August/September 2024

Subject: Probability Theory &amp; Stochastic Process

Time: 3 Hours

Max. Marks: 70

(Missing data, if any, may be suitably assumed)

PART - A

Note: Answer all the questions.

(10 x 2 = 20 Marks)

1. State Joint Conditional probability
2. Write axiomatic definition of probability.
3. A box contain 4 white balls and 6 red balls .what is the probability that 3 balls are picked at random contain at least two should be red .
4. What is a random variable? Explain the different types of random variable
5. Define correlation and covariance of two random variables X and Y.
6. If X and Y are independent, then show that  $E[XY] = E[X] \cdot E[Y]$
7. State Cross correlation
8. What is Gaussian random variable?
9. Write moment generating function.
10. A Continuous RV has a pdf  $f(x) = A e^{-x}$ . if  $x \geq 0$  .Determine the constant A .

PART - B

Note: Answer any five questions.

(5 x 10 = 50 Marks)

11. State and prove Baye's theorem.
12. The Probability Density Function (pdf) of a continuous random variable X that can take values between  $X = 1$  and  $X = 4$  is given by  $f(x) = k \cdot (1+x)$  Find (i) k (ii) Mean (iii) Variance
13. If a continuous RV 'X' has a pdf  $f_X(x) = 2x$ ;  $0 < x < 1$ . Find the pdf of Y such that  $Y = 4X^4$ .
14. Find the marginal density function of joint density function  
 $F_{xy}(x,y) = 8xy$  where  $0 \leq x \leq 1$   $0 \leq y \leq 1$
15. Consider a random process  $x(t) = A \sin(\omega t + \phi)$  where A and  $\phi$  are statistical independent and  $\phi$  is uniform in the interval of  $(0, 2\pi)$  .Is the process WSS or not ?
16. a) Derive the expressions for mean & variance of binomial random variable.  
b) Write short notes on (i) Central limit theorem (ii) State wss process
17. a) State covariance and its properties .  
b) State conditional probability distribution and properties of it